
A. Sedlazeck\textsuperscript{1} and R. Koch\textsuperscript{1}

\textsuperscript{1}Institute of Computer Science, Christian-Albrechts-University of Kiel, Germany

Abstract
When adapting computer vision algorithms to underwater imaging, two major differences in image formation occur. While still traveling through the water, light rays are scattered and absorbed depending on their wavelength, creating the typical blue hue and low contrast in underwater images. When entering the underwater housing of the camera, light rays are refracted twice upon passing from water into glass and into air. We propose a simulator for both effects based on physical models for deep sea underwater images captured by cameras in underwater housings with glass port thicknesses in the order of centimeters. Hence, modeling refraction by explicitly computing the correct path of the rays allows to accurately simulate distortions induced by underwater housings. The Jaffe-McGlamery model for effects on color is often used in computer vision algorithms as a base for simplification. We extend this model to incorporate color images, shadows, and several light sources.


1. Introduction

When working with underwater images in the area of computer vision, two fundamental differences between image formation in air and image formation in water need to be considered. First, while still traveling through the water body, light rays are attenuated and scattered [Mob94], the former leading to a loss of photons, while the latter leads to a gain of photons. Both effects are dependent on the wavelength and thus effect the colors, being responsible for the bluish/greenish colors typical for underwater images. Secondly, light rays are refracted at the water-air interface [Hec05] of the camera housing, causing geometrical distortions in the image.

Both effects cause classic computer vision algorithms to have difficulties when being applied to underwater images, and therefore require those algorithms to be adapted to the special scenario. For example the computation of a panorama or of 3D structure from a moving camera (Structure from Motion, SIM [HZ04]) requires to match correspondences between images and the use the implicitly contained geometric information for computing the camera poses. Deteriorated colors effect the feature matching while refraction causes a violation of the assumed pinhole camera model (fig. 1), thus applying established algorithms to underwater images is at best difficult. When researching suitable adaptations, simulated underwater images with known, exact ground truth are a huge advantage, when it comes to testing the algorithm adaptations. We therefore present a renderer for underwater images, simulating both, color and geometrical effects using physical models in order to gain accurately simulated underwater images, with known parameters for the physical models.

The change in colors is simulated by the Jaffe-McGlamery model [Jaf90], [McG75], often used as a basis for computer vision algorithms for color restoration, e.g. [TOA06], [SK04], [TS08]. The model used in [NCB09] can be derived from the Jaffe-McGlamery model by integrating the backscatter component, as was shown in [SK04].

For our simulator, the Jaffe-McGlamery model is extended in order to incorporate several light sources, render shadows, and uses a parametrized volume scattering function. The change in the geometry induced by the glass inter-
2. Related Work

In the literature, a multitude of methods for rendering water or participating media in general exist. Consequently, there are different approaches to rendering effects of water on light. Photon maps are used by several authors, mainly when rendering scenarios including caustics, refer for example to the work of Jensen et al. [JC98]. [GSMA08] use a bio-optical model including absorption, elastic and inelastic scattering and then also use photon mapping in order to render their images. Others, like [Mob94] solve the radiative transfer equation analytically.

A lot of papers are concerned with rendering the ocean surface including waves. In order to compute the correct water color however, models for underwater light propagation need to be used as well, even if they can be grossly simplified for this purpose. Refer to [DCGG11] for a recent overview, or to [PA01] for a model for underwater light propagation, which is a simplification of the Jaffe-McGlamery model.

Numerous recent papers target rendering underwater images close to the surface at water depths which the sunlight can reach. In those cases, effects like shafts of light and caustics are of interest for rendering. Exemplary papers are [IDN02] and [CP09].

In our case, we need a simulator using a physical model. However, instead of finding a solution to the radiative transfer equation, we decided to use the Jaffe-McGlamery model, due to it being the basis of a lot of existing computer vision algorithms. Comparable approaches, where the volume is divided into voxels and/or point spread functions are used for blurring, can also be found e.g. in [PARN04] or [CSCS02]. Another advantage of the Jaffe-McGlamery model is that it can easily be combined with the refractive camera model, which will be described in the next section.

3. Refractive Camera Model

The derivation of the ray cast in the physical underwater model (fig. 2), presented here, is essentially the same as derived by Kunz and Singh in [KS08] with slight differences in the port parametrization. When using a flat port in front of an underwater housing, the distance to the port, the glass thickness, and the normal of the glass surface within the camera coordinate system are important parameters. Here, the inner interface plane is parametrized by $\Pi_1 = (n_1, n_2, n_3, -d)$ containing the normal vector and the port’s distance to the origin. In addition, the outer interface plane is parametrized by the same normal vector and glass thickness $d_g$: $\Pi_o = (n_1, n_2, n_3, -(d + d_g))$ (refer to figure 2). When unprojecting (a camera projects 3D points to 2D points in the image plane, while unproject denotes the computation of 3D points or rays from 2D points) an image point, the goal is the computation of the point on the outer interface plane and...
the direction of the ray in water. First, an image point is un-projected to the unit length ray within the camera’s underwater housing \( \hat{X}_w \), using the camera’s intrinsic parameters including radial distortion. This ray is in the camera coordinate system, meaning that the center of projection is in the origin. In order to find the intersection \( X_i \) between ray and interface the following equation is used:

\[
\Pi^T \begin{pmatrix} \lambda_g \hat{X}_g \\ \lambda_g \hat{E}_g \\ \lambda_g \hat{Z}_g \\ 1 \end{pmatrix} = 0 \quad \Rightarrow \quad \lambda_g = \frac{d}{\langle \hat{n}_i, \hat{X}_i \rangle} \quad (1)
\]

\[
\Rightarrow X_i = \lambda_g \hat{X}_g.
\]

The intersection of the port’s inner plane and the ray, parametrized by \( \lambda_g \), is used to determine the point on the inner plane of the interface \( X_i \). In order to compute the ray within the glass, the incidence angles \( \theta_i \) and \( \theta_e \) are computed. The angle \( \theta_i \) between normal and incident ray before refraction is derived by the scalar product between the plane’s normal \( \hat{n}_i \) and the ray in air, then Snell’s law \cite{Hec05} is applied to compute \( \theta_e \):

\[
\theta_i = \arccos \left( \frac{\langle \hat{n}_i, \hat{X}_i \rangle}{||\hat{n}_i|| ||\hat{X}_i||} \right) \quad \Rightarrow \quad \theta_e = \frac{\sin \theta_i}{\mu} \quad (2)
\]

Now, the ray being incident upon the inner interface plane needs to be rotated/refracted. This rotation is described by a rotation around the normal resulting from the cross product of the plane normal and the incoming ray. With \( \theta_{\text{rot}} = \theta_e - \theta_i \), the unit quaternion for the rotation can be defined:

\[
n_{\text{rot}} = \frac{\hat{n}_i \times \hat{X}_i}{||\hat{n}_i|| ||\hat{X}_i|| \sin \theta_i} \quad \Rightarrow \quad q = \left( \frac{\sin(\theta_{\text{rot}})}{||\hat{n}_i|| \sin \theta_i}, \cos \left( \frac{\theta_{\text{rot}}}{2} \right) \right) \quad (3)
\]

This quaternion is applied to the ray \( \hat{X}_i \), yielding the refracted ray \( \hat{X}_e \), which describes the light’s traveling direction within the glass. Now, the point on the outer interface is computed:

\[
X_0 = X_i + \lambda_a \hat{X}_e \quad \text{with} \quad \lambda_a = \frac{d_0 + d - \langle \hat{n}_e, X_0 \rangle}{\langle \hat{n}_e, \hat{X}_e \rangle} \quad (4)
\]

The ray within the glass is refracted again, using the indices of refraction for glass and water, the cross product, and the unit quaternion rotation. The result is the ray in water \( \hat{X}_w \).

The 3D point can be computed if the distance \( \text{dist} \) between the camera center and the 3D point is known. The following equation can be solved for \( \alpha_w \), yielding the distance the ray needs to travel from the camera center to the 3D point:

\[
||X_0 + \alpha_w \hat{X}_w|| = \text{dist} \quad \Rightarrow \quad X_w = X_0 + \alpha_w \hat{X}_w. \quad (5)
\]

\( X_w \) is still in the camera coordinate system, but using the transform of the camera with rotation and translation, the point can easily be transformed into the world coordinate system. Figure 3 gives an overview of the whole system. This section described how the ray in water is computed, given a completely defined camera (top two boxes in figure 3). After intersecting the water ray with the 3D structure, the radiometric model needs to be applied, which is described in the next section.

### 4. Color Model

In this section the model for the change in color due to absorption and scattering will be described. The basic model is the Jaffe-McGlamery model \cite{Jaf90,McG75}, upon which many computer vision algorithms are based.

#### 4.1. Absorption

While traveling through a volume of water, photons can be absorbed by differently sized particles, like water molecules, dissolved salt, yellow matter (dissolved organic particles), phytoplankton, or anorganic particles caused by erosion and similar processes. These groups of matter cause photons to be absorbed to a different degree depending on the photon’s wavelength and the particle concentration. For each group of matter, absorption is parametrized by the absorption coefficient, describing how much light per traveling distance is absorbed. However, instead of modeling all effects separately, the sum of all absorption coefficients as the overall absorption coefficient.

\[
\tau = \sum \frac{\mu_i}{n_i}
\]

where \( \mu_i \) is the absorption coefficient of the different groups of matter and \( n_i \) is the concentration of the group.

\[
\Phi = \frac{\Phi_0}{\exp(-\tau d)} = \frac{\Phi_0}{\exp(-\sum \frac{\mu_i}{n_i} d_i)}
\]

is the radiance after traveling \( d \) distance through the water column. Here the index \( i \) is the group of matter, \( d_i \) is the thickness of the body, and \( \Phi \) and \( \Phi_0 \) are the radiance after and before traveling the distance.

The radiance \( \Phi \) is absorbed by the particulate matter, which is described by the Jaffe-McGlamery model.

\[
\Phi = \Phi_0 \exp(-\sum \frac{\mu_i}{n_i} d_i)
\]
absorption coefficient \( a \) in \([m^{-1}]\) is used. This coefficient is depending on the wavelength \( \lambda \):

\[
E(\varepsilon, \lambda) = E(0, \lambda)e^{-a(\lambda)} \quad [Wm^{-2}]
\]

with \( E(0, \lambda) \) being the irradiance before traveling any distance through the water, \( \varepsilon \) being the distance traveled, and \( a \) being the spectral absorption coefficient depending on the wavelength \( \lambda \).

### 4.2. Scattering

Apart from being absorbed, when colliding with molecules or other matter, photons can also be scattered, meaning the photon’s direction is changed after the collision. The volume scattering function (VSF, fig. 4) describes how much light is scattered towards a certain angle \( \psi \in [0, \pi] \) by \( \beta(\psi, \lambda) \) in \([sr^{-1}m^{-1}]\). Integrating \( \beta(\psi, \lambda) \) in all directions yields the scattering coefficient, the equivalent to the absorption coefficient:

\[
b(\lambda) = 2\pi \int_0^{\pi} \beta(\psi, \lambda) \sin \psi d\psi \quad [m^{-1}]
\]

which describes the loss of photons from a beam of light into all directions per distance. Both, absorption and scattering coefficient add up to form the attenuation coefficient:

\[
c(\lambda) = a(\lambda) + b(\lambda) \quad [m^{-1}]
\]

Scattering is a two-folded phenomenon. Light is scattered out of the beam, causing a decrease in irradiance. In addition, multiple scattering events also cause photons to be scattered into a beam of light causing an increase of irradiance. The loss is simply modeled using the scattering coefficient \( b(\lambda) \) in

\[
E(\varepsilon, \lambda) = E(0, \lambda)e^{-\varepsilon b(\lambda)}.
\]

Modeling the gain is more complicated: scattering is often partitioned into forward scattering \( \psi \in [0, \pi/2] \) and backward scattering \( \psi \in [\pi/2, \pi] \). Several models exist that show, that forward scattering happens mostly in the very small angles at the beginning of the interval and is therefore approximated by a linear filter [Vos91], which is in essence a low pass filter [SK04].

Modeling backward scatter is more elaborate and involves using the volume scattering function explicitly, which is why it needs to be parametrized. Measuring the volume scattering function in natural water bodies is difficult, however some widely used measurements for reference exist in the literature [Pet72]. Those measurements are used to verify different parametrizations of the VSF as described in [Mob94]. We decided to use a combination of the Einstein-Smoluchowski and the Kopelevich parametrization. The Einstein-Smoluchowski model describes sea water scattering without particles with the model equation for the volume scattering function:

\[
\beta_w(\psi, \lambda) = \beta_w(90^\circ, \lambda_0) \left(\frac{\lambda_0}{\lambda}\right)^{4.32}
\]

where values for \( \lambda_0, \beta_w(90^\circ, \lambda_0) \), and the final \( b(\lambda) \) as well as a model description can be found in [Mob94]. The Kopelevich model is used to add scattering at large and small particles in the water:

\[
\beta(\psi, \lambda) = \beta_w(\psi, \lambda) + v_s \beta^*_s(\psi) \left(\frac{\lambda_0}{\lambda}\right)^{-1.7} + v_l \beta^*_l(\psi) \left(\frac{\lambda_0}{\lambda}\right)^{0.3}
\]

where \( v_s \) and \( v_l \) are the volume concentrations of small and large particles respectively, and \( \beta^*_s(\psi) \) and \( \beta^*_l(\psi) \) the volume scattering function for small and large particles per unit volume concentration. Values for a discrete set of angles for the \( \beta^*_s \) are given and interpolated, the concentrations \( v_s \) and \( v_l \) can be varied.

Both scattering and absorption are modeled in the Jaffe-McGlamery model.

### 4.3. Jaffe-McGlamery Model

Jaffe’s work [Jaf90] was motivated by the development of a simulator for the design of underwater imaging systems. The goal in our case is developing a simulator for underwater images to be used for testing different computer vision algorithms on underwater images. Therefore, we adopt the model to incorporate color, several light sources, and shadows. In order to model the imaging process with consideration of attenuation and scattering, the irradiance being incident up on the pixel sensor is considered to be the sum of three different components:

\[
E_I(total) = E_I(direct) + E_I(fowardScatter) + E_I(backScatter)
\]

The following paragraphs describe each component. Due to the refractive camera model introduced above, which now
needs to be incorporated into the Jaffe model, the distance between camera and object is considered to be the measured distance between object and glass interface of the camera’s housing, which is the natural definition due to it being the actual distance the light traveled through water.

**Direct Light (Signal)** Light that travels directly from the light source to the object, is reflected and travels directly to the camera, while being attenuated on the way is investigated in this section. As already mentioned, attenuation unifies two effects: absorption and scattering of photons out of the beam described by the attenuation coefficient c. We adapt the model to deal with several light sources \( L \), \( j < M \) and use point light sources, being described by a position in space and their power, depending on the wavelength \( \lambda \), \( L_j(\lambda) \) in \([W]\). For the geometric computation, a point \( X \) is unprojected to a ray in water as described above. The ray is then intersected with the structure yielding the point \( X \) (fig. 3). Light from a point light source \( L_j \) only reaches the camera if there is no other part of structure shadowing \( X \). The irradiance being incident upon the structure is then (fig. 5):

\[
E_j(X, \lambda) = \sum_{j < M} E_j(1 - c(\lambda)R_j) L_j(\lambda) \cos \gamma_j \frac{1}{R_j} \delta c(\lambda)R_j \]

with \( X \) denoting the coordinates on the structure in 3D space, \( R_j \) is the distance between the light source and \( X \), \( \gamma_j \) is the angle between the ray from the light source \( L_j \) and \( X \), and the structure’s normal.

As described above, small angle forward scattering adds to the irradiance \( E_j \). In the Jaffe-McGlamery model, such light, being scattered forward at small angles, is generally modeled linearly by convolution:

\[
E_i(X, \lambda) = E_i(X, \lambda) * g(x|R_j, G, c(\lambda), B) + E_i(X, \lambda) \]

\[
g(x|R_j, G, c(\lambda), B) = e^{-(\lambda R_j)} - e^{-((\lambda R_j)^2)} \]

with \( g \) being the filter mask dependent on the two empirical values \( G \) and \( B \), and \( F^{-1} \) being the inverse Fourier transform. \( R_j = \sum_{j=M}^{1} R_{Sj} \) is the mean of all distances \( R_{Sj} \) for the different light sources, an addition to be able to incorporate several light sources. Using the linearity of convolution, this approximation allows modeling several light sources with low computational overhead. Since parts of this convolution are modeled by empirical parameters and Scheckner and Karpel [SK04] noted that the linear convolution is a low pass filter, we approximate (14) with a Gaussian filter, for which the filter mask depends on the distance the light traveled. The amount of forward scatter added is weighted by one empirical factor \( K \) similar to [TOA06].

In order to compute the reflected light and attenuate it properly, the Jaffe-McGlamery model uses a reflectance map \( M(X) \), which is embedded in the x-y-plane of the coordinate system. Instead, we use only one reflectance coefficient \( M \), and can model arbitrary 3D structures specified by 3D models. While traveling from the structure to the camera after reflection, the light is attenuated again. In addition, the camera itself is usually no ideal pinhole camera and effects like vignetting, f-number, and lens transmittance are combined in the fundamental radiometric relation, which turns scene radiance into irradiance incident upon the pixels of the sensor [Sze11]:

\[
E_d(x, \lambda) = \frac{\pi}{4f_n R_{c}^2} E_s(\lambda)\cos \theta |(R_c - F_j)^2 \pi| \]

with \( R_c \) being the distance between \( X \) and the camera. The angle \( \theta \) is used to describe the angle between the incoming ray and the camera’s optical axis. The cosine term models vignetting (refer also to [Sze11]), \( T_o \) is the lens transmittance, \( f_n \) the camera’s f-number, and \( F_j \) is the camera’s focal length in mm.

**Forward Scatter (Signal)** The forward scattered part of the signal can easily be derived as seen above, using the distance dependent Gaussian filter:

\[
E_{fs}(x, \lambda) = E_d(x, \lambda) * g(x|R_c, G, c(\lambda), B) \]

The irradiance of the signal incident upon pixel \( x \) has now been derived including the proportion of light coming directly from the light source into the camera via reflection on the object and including part of the scattering proportion, namely, a proportion of small angle forward scattering. Small angle forward scattering has been found to increase signal irradiance, but mainly cause the image to blur depending on the distance between camera and object.
Backscatter (Veiling Light) The part that is still missing, is backscatter. Light is scattered in all directions multiple times, even one light source has numerous beams that loose photons due to scattering, which can then be scattered into other beams. Those scattering events happen so often that backscatter can be viewed as some kind of ambient or veiling light being present in the water in vicinity to a light source or close to the water surface during the day.

As stated in McGlamery’s work, the 3D-space through which the back scatter is accumulated, is sliced into \( N \) planes of thickness \( \Delta z \), that are parallel to the camera’s image plane. For each of those planes, the amount of irradiance incident upon it due to backscatter, can be computed similar to above, including the forward scattered amount of light. After that, the irradiance based on the back scatter portion of the light, is the superposition of all the slices. Again, the original model is extended to incorporate several light sources for backscatter computation. This creates the need of applying the VSF to the irradiance on the backscatter plane at this point instead of later as in the original model, which is possible due to the linearity of convolution. The result is:

\[
E_s(x') = E_{s, d}(x') + E_{s, fs}(x') \quad \left[ \text{Wm}^{-2} \text{sr}^{-1} \text{m}^{-1} \right]
\]

(17)

where \( \Delta z \) denotes the thickness of the back scattering volume slice, \( Zbsi \) is the distance between the center point of the slice \( i \) and the camera, and \( i \) is the index of the back scatter slab. (18) can again be split into a scene radiance part due to backscatter and a camera transmission part, identical to the one in (15), which transfers scene radiance into pixel irradiance (refer also to fig. 3).

Wavelengths The effects described above are wavelength dependent. This is especially true for the absorption and scattering coefficients. The natural extension of the Jaffe-McGlamery model to incorporate colors, is modeling the 3 color channels using 3 discrete bands of frequencies for \( \lambda \), with wavelengths according to the color channels. This concludes the model introduction. The next section will present some rendering results.

5. Results

Due to the need of using our own camera model, it was difficult using ready-made software packages for the implementation. Therefore, we build upon BIAS (www.mpi-informatik.uni-kiel.de) and the Open Source library OpenSceneGraph (www.openscenegraph.org/projects/osg) in order to build the renderer. The run-time for rendering one image is in the order of a few minutes, however, we never targeted at running in real-time being close to the physical models was of greater importance. The motivation for
the simulator was creating synthetic images as captured by a ROV. ROVs usually carry a set of lamps attached to the front of the frame, often at the top, but approximately in the same plane as the camera. Our implementation contains an editor allowing to create a set of such lamps, which can be positioned very close to the camera, but also be moved further away.

In order to test the simulator, we build a synthetic model of an underwater scene and added a cube with a checkerboard pattern. Figure 6 shows the different components from the rendering process. The surface rendering clearly shows the shadows produced by 3 lamps to the upper right of the camera. Geometric ground truth is rendered in form of depth maps recording the camera-3D point distance for each pixel. The fourth image shows the light that is incident on the structure including the texture and reflection. After adding forward scatter and attenuating on the way to the camera, the signal (fifth image) results. The first backscatter plane is not yet occluded by the structure and clearly shows the decrease of the backscatter with growing distance from the light source. In the result image, the background structures are visible in contrast to the signal image because they are illuminated by the backscatter.

5.1. Backscattering Effects
Rendering results for this scene with increasingly turbid water, e.g. increasing backscatter, can be seen in figure 7. The left column shows the backscatter component, while the right column shows the complete rendering result. As can be noticed, the contrast diminishes with growing concentration of scattering particles. One of the major conclusions in [Jaf90] concerned the placement of the lamps relative to the camera and the type of lamp in order to receive usable images from deep sea environments: there is always a compromise between contrast and power reaching the imaging system due to backscatter and attenuation. This can be observed in figure 8, where the lamp was moved away from the camera up to a distance of approximately 2m.

5.2. Refractive Effects
If the necessary underwater housing is modeled explicitly, strong refractive effects are visible in the image. In addition, the object appears to be enlarged by a factor of 1.333, the index of refraction of water. Both effects can be observed in fig. 9 when comparing the left image (with underwater...
housing) with the right image (no underwater housing. In the left image, the cube not only appears to be closer, but is also distorted at its edges. The underwater housing in this case was parametrized with a glass thickness of 4 cm, the interface distance was 2 cm, and the interface normal was rotated by 0.1°.

6. Conclusion and Future Work

We have presented a renderer for deep sea underwater images that utilizes two physical models, one for light propagation within the water and one for refracting the light rays at the underwater housing. In order to achieve realistic images, the Jaffe-McGlamery model has been extended to incorporate color channels and several light sources. In addition, shadows can be rendered. Explicitly modeling refraction at the water-glass-air interface allows to render the distortion effects typical for underwater images. The simulator therefore serves as a basis for generating underwater images with known ground truth compliant to the physical models that can be used to develop or adapt and evaluate computer vision algorithms for underwater scenarios.

In the future, we plan to improve efficiency by parallelizing the computation and to model material properties other than diffuse reflection. In addition, floating particles can add more realism. The simulator will be utilized in order to develop a Structure-from-Motion system that can incorporate refraction and does not break down due to the low contrast common in underwater images. This computer vision system uses the refractive camera model described and simulated here.

References


